Adversarial Network Optimization under Bandit Feedback: Maximizing Utility in Non-Stationary Multi-Hop Networks

Yan $\mathsf{Dai}^{1\leftarrow 2}$







Stochastic Network Optimization (SNO)

Dynamically allocates resources in networks to fulfill demands, with strong & rigorous performance guarantees including

- Throughput Maximization, *e.g.*, [Tassiulas and Ephremides, 1992; 2002; Dai and Lin, 2005; Shah and Shin, 2012], ...
- Delay Minimization, e.g., [Eryilmaz and Srikant, 2007], ...
- Utility Maximization, *e.g.*, [Neely et al., 2005; Georgiadis et al., 2006; Jiang and Walrand, 2009], ...
- as well as numerous successful applications including
 - Wireless Networks [Lin and Shroff, 2006; Srikant and Ying, 2013]
 - Cloud Computing [Meng et al., 2010; Maguluri et al., 2012]
 - Supply Chain Management [Rahdar et al., 2018]

From SNO to ANO Model & Objective

Key Limitations of Vanilla SNO

Despite huge success, vanilla SNO faces critical limitations:

Limitation 1: Stationary Assumption

- Classical SNO requires network conditions (*e.g.*, arrival / service rates, capacities) to be *stationary over time*
- Fails in reality: auto driving, mobile networks, DDoS, ...
- ⇒ Consider Adversarial Network Optimization (ANO)

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Limitation 2: Full Prior-Decision Information

- Many existing network optimization works also require network conditions to be known a-priori
- Fails in reality: underwater communication, IoT sensors, ...
- $\bullet \Rightarrow Consider \textbf{ Bandit Feedback Models}$

From SNO to ANO Model & Objective

Challenges and Main Contributions

(Q). Can we maximize utility in adversarial & multi-hop networks only using bandit feedback?

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Our Contribution: UMO^2 (<u>U</u>tility <u>Max via OLO & BCO</u>)

- First algorithm to answer (Q), with rigorous utility & stability guarantees
- Roadmap: Online Learning for ANO
- Novel OL algs of independent interest

Challenges and Main Contributions (Cont'd)

(Q). Can we maximize utility in adversarial & multi-hop networks only using bandit feedback?

	Network	Arrival &	Tanalagu	Objective	1 1+:1:+
	Conditions	Jervice	Topology	Objective	Othity
[Neely et al., 2005]	Stochastic	Known	Multi-Hop	Utility Maximization	Known
[Neely, 2010]	Adversarial	Known	Multi-Hop	Utility Maximization	Known
[Liang and Modiano, 2018b]	Adversarial	Known	Multi-Hop	Network Stability	_
[Liang and Modiano, 2018a]	Adversarial	Known	Multi-Hop	Utility Maximization	Known
[Yang et al., 2023]	Adversarial	Unknown	Single-Hop	Network Stability	_
[Huang et al., 2024]	Adversarial	Unknown	Single-Hop	Network Stability	_
Ours	Adversarial	Unknown	Multi-Hop	Utility Maximization	Unknown

Table: Comparison with Most Related Works

Introduction From ur Approach Mode

From SNO to ANO Model & Objective

Our Setup: ANO with Bandit Feedback



• Multi-Hop Network $\mathcal{G} = (\mathcal{N}, \mathcal{L})$; *T*-round planning

Introduction From SNO to ANC Our Approach Model & Objective

Our Setup: ANO with Bandit Feedback



Utility func gt adversarial & unknown

- Multi-Hop Network $\mathcal{G} = (\mathcal{N}, \mathcal{L})$; *T*-round planning
- Arrival Decision $\lambda(t)$ under adv & unknown utility func $g_t(\lambda(t))$

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Introduction From SNO to ANC Jur Approach Model & Objective



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Introduction

Model & Objective



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Online Learning for ANO: 3-Step Punchline

Q Reduce to Online Learning via global Lyapunov analysis

• single Lyapunov term is too sensitive to adversarial corruptions

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Network Stability & Online Linear Optimization Utility Maximization & Bandit Convex Optimization

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- single Lyapunov term is too sensitive to adversarial corruptions
- **Obsign** novel *queue-based OL* for ANO-specific challenges
 - \bullet unbounded queue lengths \Rightarrow unbounded loss magnitudes



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Online Learning for ANO: 3-Step Punchline



- single Lyapunov term is too sensitive to adversarial corruptions
- **Obsign** novel *queue-based OL* for ANO-specific challenges
 - \bullet unbounded queue lengths \Rightarrow unbounded loss magnitudes
- **Solution** Extend OL guarantees to ANO via self-bounding analysis
 - $\mathbb{E}[\sum_t \|\boldsymbol{Q}(t)\|_1] \leq T^{1/4} \mathbb{E}[\sqrt{\sum_t \|\boldsymbol{Q}(t)\|_2^2}] \Rightarrow$ network stable



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Algorithms & Analysis Outlines

In each round $t = 1, 2, \dots, T$

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Figure: NSO for Network Stability

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Network Stability \Rightarrow Online Linear Optimization

Step 1: Reduction via Global Lyapunov Analysis

Stability min $\mathbb{E}\left[\sum_{t} \|\boldsymbol{Q}(t)\|_{1}\right]$

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Step 1: Reduction via Global Lyapunov Analysis

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Step 1: Reduction via Global Lyapunov Analysis

Stability min
$$\mathbb{E}\left[\sum_{t} \|\boldsymbol{Q}(t)\|_{1}\right]$$

 \downarrow (Global Lyapunov drift analysis)
 $\forall (n,m) \in \mathcal{L}, \min \mathbb{E}\left[\sum_{t} \langle \underbrace{\boldsymbol{a}_{n,m}(t)}_{\text{Decision}}, C_{n,m}(t)(\boldsymbol{Q}_{m}(t) - \boldsymbol{Q}_{n}(t)) \rangle\right]$

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Network Stability \Rightarrow Online Linear Optimization

Step 1: Reduction via Global Lyapunov Analysis



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Network Stability \Rightarrow Online Linear Optimization

Step 1: Reduction via Global Lyapunov Analysis

$$\begin{aligned} & \mathsf{Stability} \ \min \ \mathbb{E}\left[\sum_{t} \| \boldsymbol{Q}(t) \|_{1}\right] \\ & \downarrow \quad (\mathsf{Global Lyapunov drift analysis}) \\ & \forall (n,m) \in \mathcal{L}, \ \min \ \mathbb{E}\left[\sum_{t} \langle \underbrace{\mathbf{a}_{n,m}(t)}_{\mathsf{Decision}}, \underbrace{C_{n,m}(t)(\boldsymbol{Q}_{m}(t) - \boldsymbol{Q}_{n}(t))}_{\mathsf{Loss Vector}} \rangle\right] \end{aligned}$$

 \implies Reduce to Online Linear Optimization (OLO)

ANO-Specific Challenges

O Unbounded Loss Magnitudes

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ANO-Specific Challenges

- **O** Unbounded Loss Magnitudes
- **Output** Negative Loss Components

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ANO-Specific Challenges

- **O** Unbounded Loss Magnitudes
- Negative Loss Components
- **3** Requires Adaptivity

Existing OLO algorithms fail to tackle all issues simultaneously.

Yan Dai and Longbo Huang

Adversarial Network Optimization under Bandit Feedback

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OLO Guarantee \Rightarrow Network Stability Guarantee

Step 2: A Novel & Customized OLO algorithm: AdaPF0L

$$\mathcal{O}\left(\sqrt{\sum_{t} \|C_{n,m}(t)(\boldsymbol{Q}_{m}(t) - \boldsymbol{Q}_{n}(t))\|_{2}^{2}}\right)$$

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$$\mathcal{O}\left(\sqrt{\sum_{t} \|C_{n,m}(t)(\boldsymbol{Q}_{m}(t) - \boldsymbol{Q}_{n}(t))\|_{2}^{2}}\right) \lesssim \mathcal{O}\left(\sqrt{\sum_{t} \|\boldsymbol{Q}(t)\|_{2}^{2}}\right)$$

allows large magnitudes, negative losses, and is adaptive

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Step 3: Self-Bounding Analysis for ANO Guarantee

Self-bounding analysis: From Steps 1 & 2, NSO ensures

$$\mathbb{E}\left[\sum_{t} \|\boldsymbol{Q}(t)\|_{1}\right] \leq \mathcal{O}(T^{1/4}) \mathbb{E}\left[\sqrt{\sum_{t} \|\boldsymbol{Q}(t)\|_{2}^{2}}\right] \leq \mathcal{O}(T^{1/4}) \mathbb{E}\left[\sum_{t} \|\boldsymbol{Q}(t)\|_{1}\right]^{3/4},$$

 $\implies \frac{1}{T} \mathbb{E}[\sum_t \| \boldsymbol{Q}(t) \|_1] = \mathcal{O}(1), i.e., \text{ network is stabilized by NSO}$

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Network Stability to Utility Maximization: Another 3 Steps



Figure: NSO for Network Stability

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Final Guarantee of UMO²

UMO² Ensures Simultaneously...

• Network Stability. Average queue length remain bounded:

$$\frac{1}{T} \mathbb{E}\left[\sum_{t=1}^{T} \|\boldsymbol{Q}(t)\|_{1}\right] = \mathcal{O}_{T}(1)$$

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• Near-Optimal Utility. Utility converges to the best "mildly varying" policy with 1/poly(T) gap (see our Thm 4.5):

$$\frac{1}{T} \, \mathbb{E}\left[\sum_{t=1}^T g_t(\mathring{\boldsymbol{\lambda}}(t)) - g_t(\boldsymbol{\lambda}(t))\right] = \mathcal{O}_T(1/\mathrm{poly}(T))$$

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^aAny forward-looking (*i.e.*, allowing offline/hindsight optimization) policy with slowly changing actions.

Main Results & Takeaway

Main Results

- First utility result for multi-hop ANO w/ bandit feedback
- General reduction framework from ANO to Online Learning
- Novel adaptive OL algs (AdaPFOL, AdaBGD) for unique network challenges (*esp.* unbounded queue & self-bounding)

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- **Obsign** novel & customized OL algs for ANO challenges
- S Extend OL guarantee to ANO via self-bounding analysis

Questions are more than welcomed!

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